

Numerical Study of Natural Convection Heat Transfer in Porous Particles Through Composite Filters

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Abstract

The study of heat transmission through porous materials within the confines of reactor configurations stands as a pivotal realm of inquiry in the realms of engineering and the applied sciences, possessing wide-ranging applications spanning from soil mechanics to the refinement of heat exchange systems. Porous substances, distinguished by their interconnected voids or interstices, present an array of reactor forms that profoundly shape the flow of fluids and the conveyance of particles within the substance. This transfer of thermal energy entails intricate mechanisms encompassing conduction, convection, and radiation, all subject to modulation by characteristics such as the thermal conductivity, porosity, and permeability of the material. Furthermore, phenomena including phase transitions, the behavior of non-Newtonian fluids, and chemical reactions occurring within the porous structure serve to further complicate the analysis. Scholars and practitioners in the field employ mathematical models, numerical simulations, and experimental methodologies to illuminate the dynamics of heat transfer, with a particular emphasis on parameters such as temperature distributions, rates of heat flux, and convective coefficients. The comprehension of heat transmission within such trapezoidal porous mediums is of paramount importance for the refinement of the design and operation of systems wherein effective thermal management stands as a necessity. This interdisciplinary domain not only fosters heightened efficiency but also fosters the propagation of sustainable practices across various sectors of industry.

Keywords: Porous media, fluid dynamics, permeability, flow diagnosis, mechanical filtration and non-Newtonian fluid

INTRODUCTION

Numerical analysis pertaining to heat transfer confined in different types of porous cavity has earned

several attentions because of its application in numerous practical areas such as solar collectors, geophysics, buoyant heat transfer in atmosphere, temperature distribution of clouds, soil properties and so on. A literature review shows a relatively recent interest in the ciphered dissection of heat transfer in enclosure.

Jiale Fu and their colleagues [1]. didst explore the traits of stratified low velocity cascade falling under the domain of the porous matter of the innermost part of engine particulate filters, employing a two-dimensional lattice Boltzmann–Cellular Automata (LB–CA) probabilistic model to simulate the flow properties of said porous substance. The study examines how dimensionless permeability varies across different numerical structures at the pore

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scale with changes in Reynolds number. It also considers implications for heat transfer and particle filtration. Findings indicate that at low Reynolds numbers ($Re < 1$), the flow behavior of various structures aligns with Darcy's law. Notably, the ordered structure exhibits a notably higher dimensionless permeability coefficient compared to the disordered structure. However, this increased permeability in the ordered structure comes at the expense of reduced filtration efficiency.

R A Dekhtyar et al [2]. investigated hydrodynamics and heat transfer under conditions of filtering of water and aqueous solution of glycerol through a porous insert in the channel was carried out. The values of the coefficient of hydraulic resistance and heat transfer for chaotic backfill of balls with a diameter of 3.2 mm for filtering water and 47% glycerol solution have been determined.

Three flow regimes were investigated: inertial, transient and turbulent. Suleiman Abu-Ein et al. [3] studied exhaust gases flow in porous media where he concluded that the gases pressure is decreased as such gases flow along the DPF unit and exhaust system such that there is pressure drop present and the temperature distribution profile shows there is a fluctuation along the DPF unit. Axial and vertical velocities were decreasing as the gases flow through the DPF unit. It is recommended to study it as non-linear 3D problem.

Henry Darcy [4-5]. has marked a momentous milestone within the field. In conducting his experiments upon the soils of France, Darcy sought to delve deeper into the mysteries of water filtration, employing silica sand as the medium of filtration. His apparatus, simple yet astute, comprised a vertical column fashioned to measure the flow of water and the pressure differential therein. The fruits of his labour were articulated in terms of the flow differential estimate with time of water and the variance in pressure across the silica sand. From such findings, Darcy didst formulate a correlation betwixt the flow rate and pressure difference, taking into account the length and breadth of the porous medium, alongside a constant. Since its inception, Darcy's law hath found widespread application in predicting the flow characteristics within porous media.

Wissam H. Khalil [6]. and his compatriots embarked upon a comprehensive study concerning the optimization of magneto hydrodynamic (MHD) free convection within a porous trapezoidal cavity adorned with a wavy bottom boundary Utilizing the venerable response surface methodology (RSM), their research dissected the influence of sundry parameters, including the undulations of the bottom wall, wave amplitudes, sidewall temperatures, the Hartmann number, and the Rayleigh number, upon the differential estimate of heat transfer with time, within the wavy trapezoidal cavity suffused with porous media and unpolluted water under the sway of a magnetic field. Employing numerical simulations and optimization analyses through the esteemed ANSYS FLUENT-CFD software in conjunction with Design of Expert V12 statistical software, their study ventured into the realm of multi-objective optimal design (MOOD) to ascertain the most felicitous configuration of the trapezoidal cavity, with a particular focus upon metrics to the same degree as the Nusselt number, heat transfer differential estimate, and enhancement of convection.

Meysam Atashafrooz [7]. and his cohorts undertook an exploration of the effects of thermal radiation, magnetic forces, and the concentration of hybrid nano particles upon the heat carrying phenomenon and fluid dynamics within an open trapezoidal enclosure distinguished by diagonal sidewalls. With meticulous attention to detail, their study delved into the ramifications of sundry parameters, including the radiative parameter, the Hartmann number, and the volume fraction of hybrid nanoparticles, upon the distributions of dimensionless temperature, velocity, and Nusselt number within the enclosure.

Mohsen Izadi [8]. and his associates embarked upon an inquiry into the charging operandi of a not wholly heated trapezoidal thermal vim cache, employing nanoscopic-broadened phase change material (PCM) and a controllable homogenous magnetic enchantment area. Their research scrutinized the repercussions of various parameters, including the Rayleigh number, Hartmann number, inclination

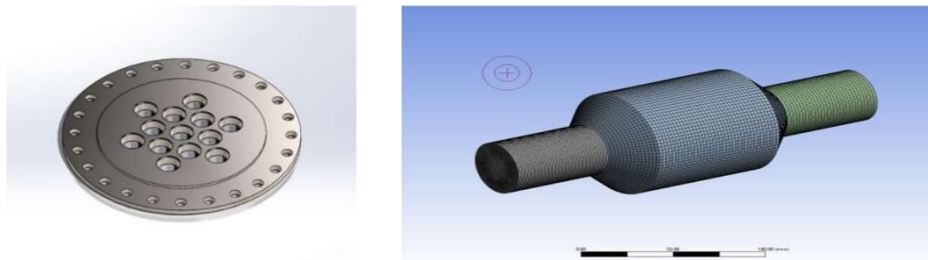
angle of the magnetic field, and cubic content unit fraction of nanoparticles, upon the melting time of the PCM and the Nusselt number. Elucidating the underlying physical mechanisms, their study provided graphical representations of the results.

Sourav Chatterjee [9]. and his collaborators examined the impact of trapezoidal cavity shapes and the positioning of inner tubes upon the melting process of PCM. Their study assessed how angular variations in trapezoidal containers and the placement of inner tubes affected the rate of melting and heat transfer of three distinct phase change materials. Concluding that optimization of cavity shape and inner tube positioning markedly enhanced the melting process and charging rate, their study identified an optimal configuration (Case-A) for all examined phase change matter or hardware, while also suggesting quiescent avenues for future research.

Chabani [10]. and colleagues delved into the convective heat transfer properties of an Ag-Al₂O₃/H₂O hybrid nanofluid, composed of a blend of nanoparticles renowned for their superior thermal characteristics. Their research explored the influence of a horizontal magnetic enchantment area upon the flow and heat transfer behaviour of the hybrid nanofluid, focusing upon variations in the Hartmann number and nanoparticle volume fraction. Additionally, their study analyzed the impingement of the enclosure's aspect ratio, wall undulation number, and side wall inclination angle upon the scorching or sweltering rendition and heat transfer characteristics of the hybrid nanofluid.

Considered Model

The physical domain is drawn with the coordinate system for the current study and presented in Figure 1 (a). The domain also shows boundary conditions. The system was two-dimensional porous circular enclosure, closed by cylindrical thermal walls. All acting lymphatic molten form properties are supposed to be constant except the coolant used for the process it can vary in temperature.



(a) Figure 1. Tubular grid (b) Mesh pattern for a cylindrical enclosure.

Mathematical Equations and Numerical Solution

The general mathematical equations are written as follows: Hydraulic Conductivity equation:

$$\frac{Q}{A} = \frac{h_1 - h_2}{L} \quad (1)$$

$$Q = -KA \frac{\partial h}{\partial x} \quad (2)$$

$$\text{Pressure Drop equation } \Delta P = -\frac{\mu}{\sigma} V + \mu_e \Delta^2 V \quad (3)$$

$$\text{Darcy equation (Momentum equation)} \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (4)$$

$$\text{Modified Rayleigh number } Ra = \frac{g \beta_T \nabla T K L}{\nu \alpha} \quad (5)$$

The Dimensional Parameters Are Given Below. Working Fluid: Air

Properties:

Density: 1.225 kg/m³
 Thermal Conductivity: 0.0242W/Mk

The aforementioned governing equations, in conjunction with the pertinent boundary conditions, are discretized employing Darcy's Law. This investigation utilizes Ansys software, incorporating a hexahedral meshing of elements. Subsequently, the pressure and velocity contours are determined and benchmarked against existing references. The quartet structure generation set, frequently referred to as the Q-set, and is a systematic approach employed in the design of digital filters. This methodology comprises a set off our complex numbers, denoted as {z1,z2,z3,z4,} which serve as the vertices of a rectangle in the z-plane. These points delineate the boundary of the region within which the poles and zeros of the digital filters are restricted.

Permeability and Grid Number

The correlation between permeability and grid resolution is crucial for guaranteeing the precision of numerical simulations concerning fluid flow in porous media. Variations in permeability within the medium necessitate finer grid resolutions to accurately capture abrupt changes. This iterative procedure also assists in validating and calibrating numerical models, ensuring they accurately depict real-world fluid flow behaviours.

As we notice in the Figure 2 after reaching a grid number of 150x150 there is hardly any increase in permeability but with the increase in number of grid number, the time taken for calculation significantly improves. There for grid number of 200 x 200 is to be considered to secure a good accuracy with reduced calculation time.

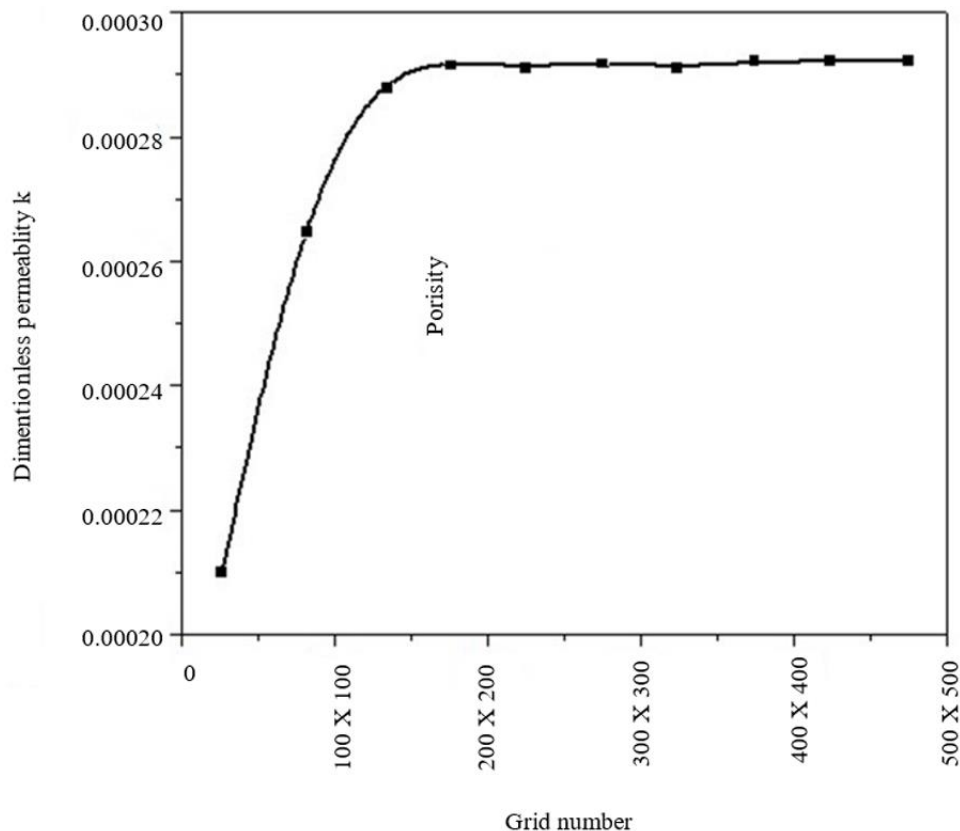


Figure 2. Grid study for dimensionless permeability.

Validation

The twin fold network framework is devised to depict both the pore interstices and the solid grain matrix of a porous substrate through intertwined networks. It facilitated the emulation of coupled heat and mass conveyance, duly considering heterogeneous temperature dispersion within both the void expanses and the solid matrix.

This framework is especially beneficial for undertakings such as catalytic reactors, micro-fluidic assays, and micro-cooling contrivances. The creators authenticate their dual network framework by juxtaposing it with three-dimensional conjugate heat transfer simulations. These simulations encompass both conduction-prevalent and convection-prevalent scenarios. The model exhibited proficiency in replicating effective thermal conductivity across a vast spectrum of fluid-to-solid thermal conductivity ratios employing a singular set of parameters.

In Figure 3, The x-axis represents porosity which is the fraction of void space in a material. A higher porosity indicates more open space within the structure. The y-axis represents the dimensionless permeability, which measures how easily a fluid can flow through the porous medium. As porosity increases, the dimensionless permeability increases for all three configurations. This is expected because higher porosity implies less resistance to fluid flow. The Parallel structure shows the steepest increase in permeability with porosity, making it the most efficient for fluid transport. The QSGS structure has the least permeability, likely due to its more restrictive geometry that inhibits fluid flow.

The dual network framework adeptly apprehended local thermal non equilibrium phenomena. For example, it is capable of emulating conditions where temperature disparities arise within the porous substrate owing to fluid-solid interactions. This is of particular pertinence in micro-cooling apparatuses and sundry other applications. Should thine analysis accord with the model's prognostications, the mayest aver that the pressure chart from the manuscript doth corroborate the findings.

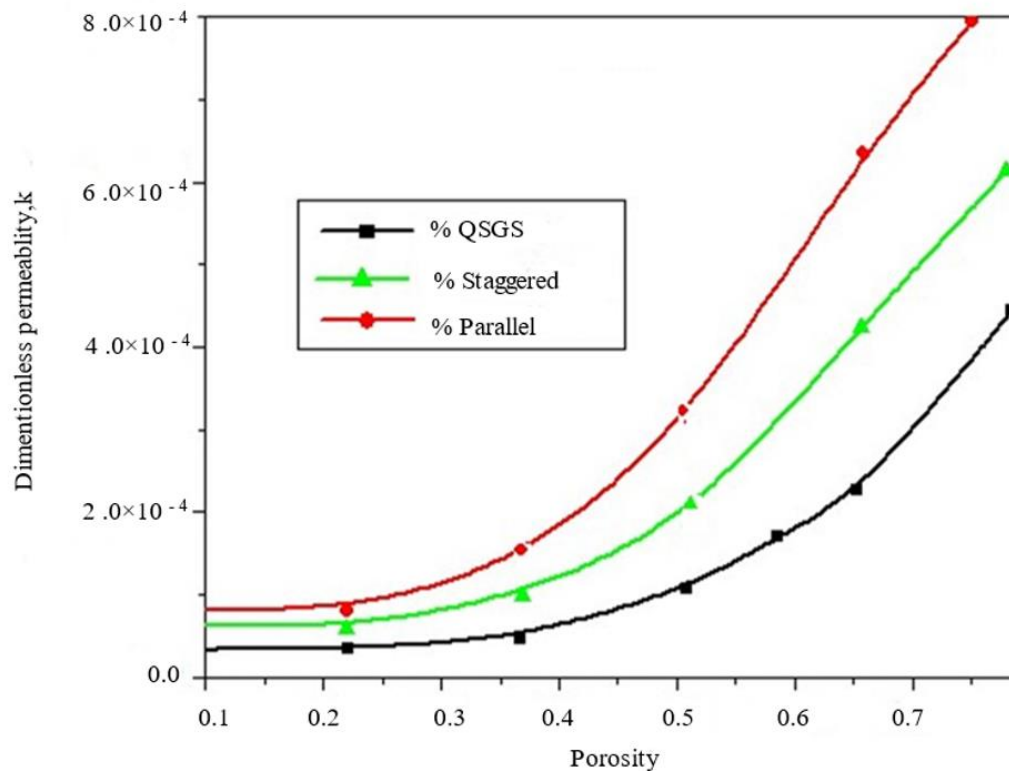


Figure 3. The validated graph between permeability and porosity.

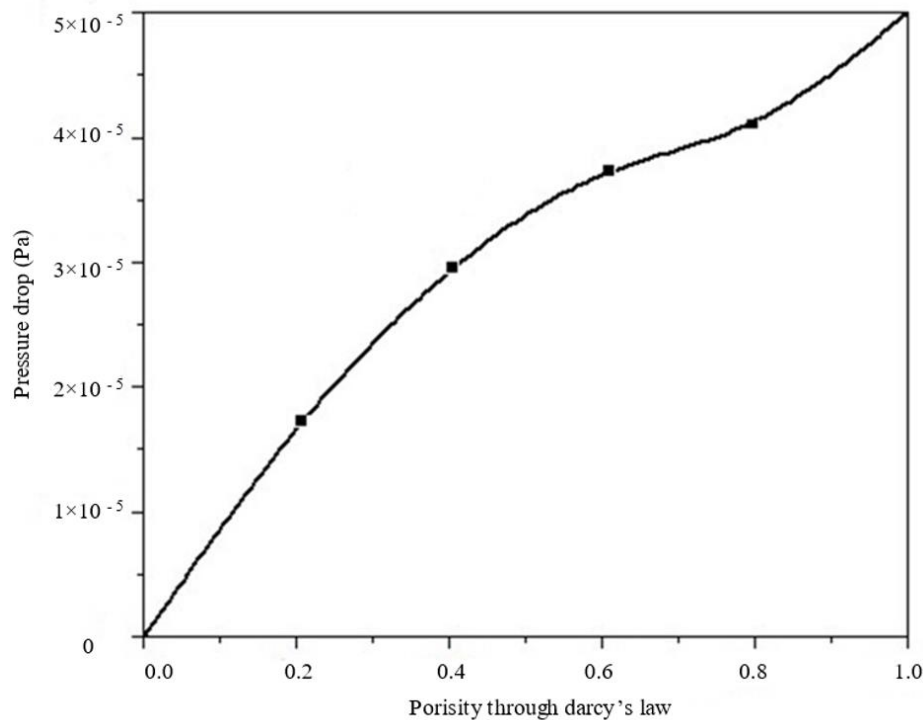


Figure 4. Validated pressure loss curve obtained through darcy's law.

In Figure 4 illustrates the relationship between porosity and pressure drop (ΔP) through a porous medium, likely based on Darcy's Law. The curve shows a positive and non-linear relationship between porosity and pressure drop. At low porosity, the pressure drop is minimal because the fluid encounters high resistance in a largely solid medium. As porosity increases, the void spaces allow more fluid flow, causing the pressure drop to increase significantly. The curve steepens at higher porosities, indicating that beyond a certain point, the rate of pressure drop accelerates with increased porosity.

The research determined that the efflux of gases through ULPA and HEPA Filters is laminar, denoted by smooth, parallel strata of fluid that remain unmixed. As the gases traverse the DPF, a discernible pressure diminution occurs, attributable to the resistance the porous medium presents to the exhaust gases' flow. The thermal distribution along the DPF unit exhibits variations, which may influence the gases' velocity and pressure.

Validation of Analytical Findings the analytical investigation delineated in the treatise "Numerical and Analytical Study of Exhaust Gases Flow in Porous Media with Applications to Diesel Particulate Filters" hath been scrupulously validated. The juxtaposition of numerical simulations with analytical resolutions reveals a profound correlation, corroborating the veracity of the methodologies employed. This validation is paramount, fortifying the credibility of the findings and their prospective application in the conception and optimization of diesel particulate filters. Ramifications for Particulate Filters The corroborated findings bear significant ramifications for the advancement of ULPA and HEPA particulate filters. The exact modeling of exhaust gases and flux through porous media permits engineers to prognosticate the behavior of particulate matter within the filters with greater precision. Consequently, this engenders the creation of more effectively, which are vital for abating emissions and conforming to rigorous environmental edicts.

Prospects for Future Research and Applications the substantiation of the study's results heralds future inquiry in the domain. It furnishes a robust foundation for examining more intricate flow scenarios and the influence of sundry parameters on the filtration process. Furthermore, the validated models may be employed in other contexts where the efflux of gases through porous media is a critical consideration, such as in catalytic converters and heat exchangers.

RESULTS

An intergerial investigation had been undertaken upon diverse kinds of filters and the flow of fluids within a porous chamber. Different types of filters were considered based on the factor to improve the Heat flux and heat absorbing capabilities of the filters. The governing parameters which effectively affect the heat transfer and fluid flow are Filters design and Rayleigh number (Ra) of the enclosure. The pores arrangement is considered to be as parallel arrangement, as there is uniform heat distribution throughout and Ra range is around 2000-4000 with porosity ranging from 0.4-0.6 such that natural convection is feasible. Here Laminar flow and turbulent flow both can be noticed which helps us in accomplishing desired results.

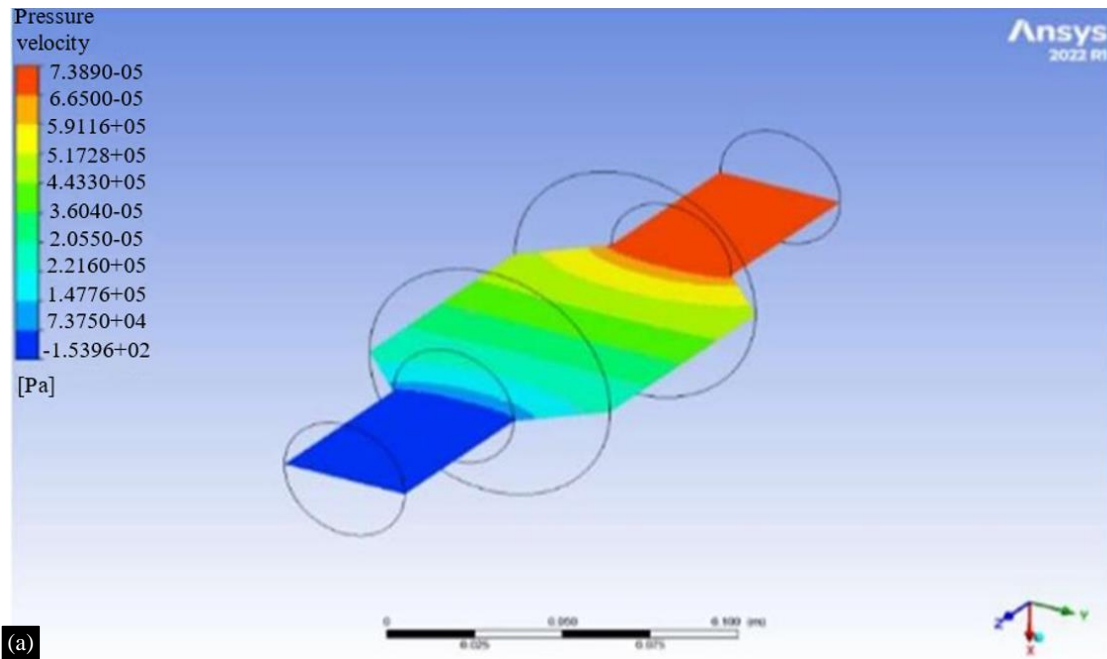
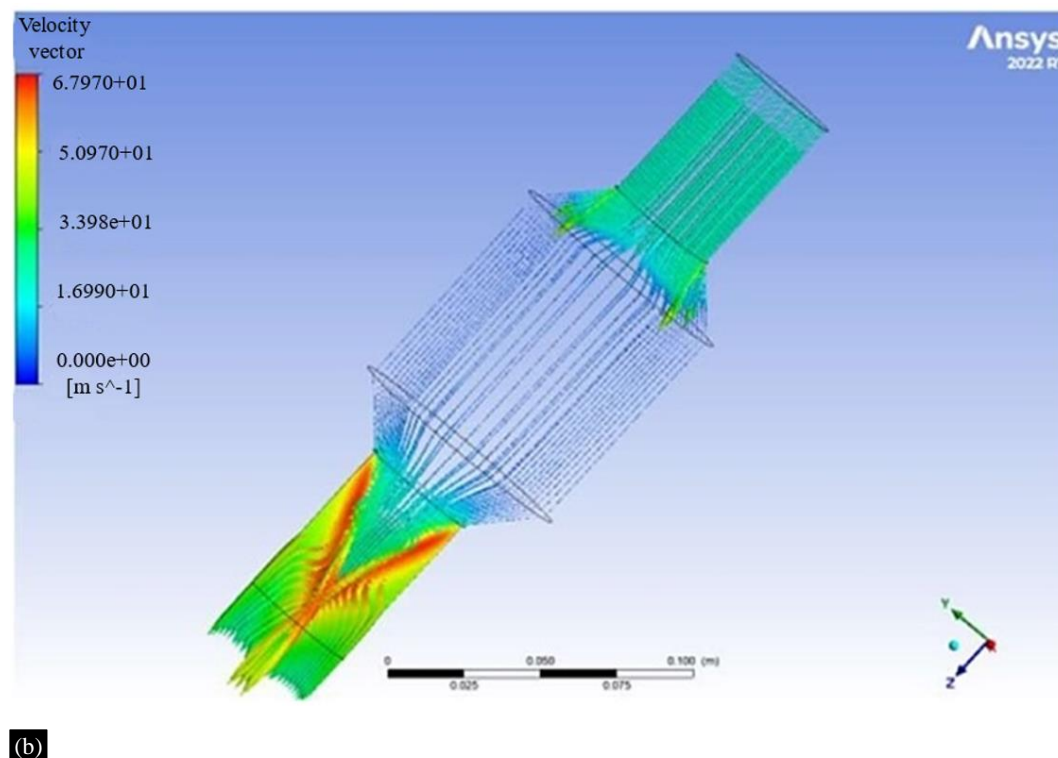


Figure 5. (a) Pressure velocity.



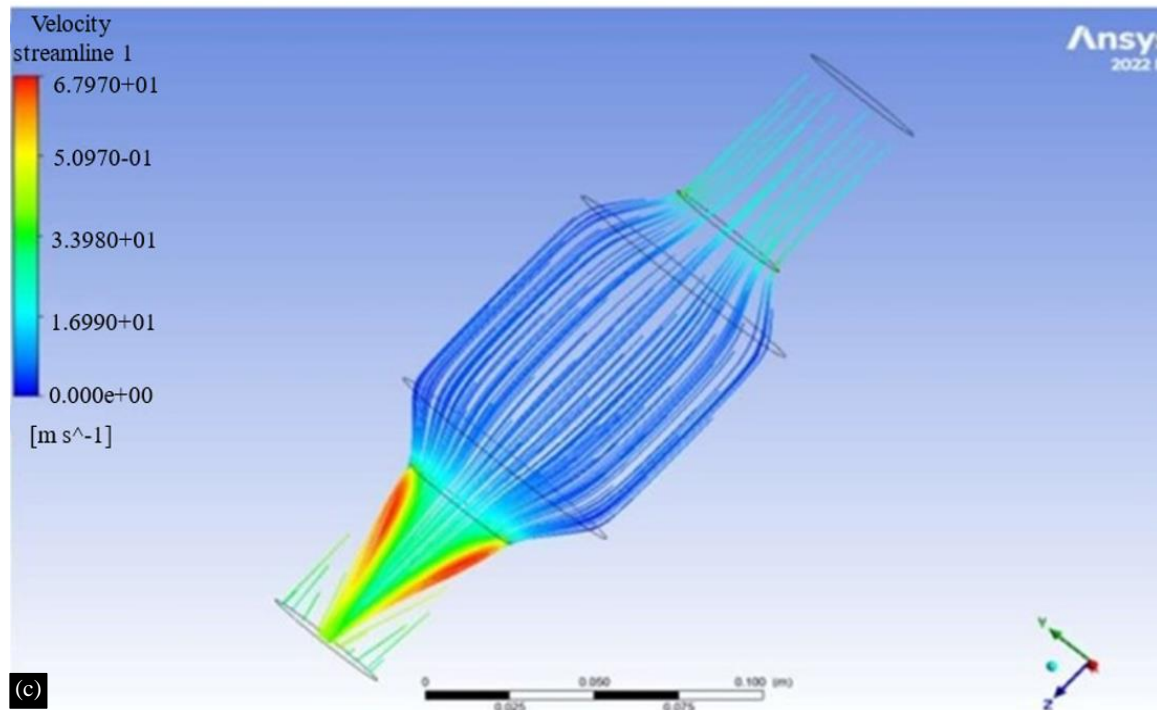


Figure 5. (a) ,(b) and (c) shows the velocity of airflow inside of the enclosure and it portrays the pressure difference and the laminar flow with a change to turbulent flow at the exit point. The red region shows how the velocity is higher at the outlet of the enclosure.

Table 1. Variation of Porosity and Heat flux for conventional filters

<i>Dh(m)</i>	Normal filters	
	<i>Porosity (ε)</i>	<i>Heat flux(q)W/m²</i>
1	0.45	0.0019
2	0.48	0.002
3	0.51	0.004
4	0.54	0.00046
5	0.57	0.0073
6	0.6	0.0077

Figure 5 (a),(b) and (c) shows the velocity of airflow inside of the enclosure and it portrays the pressure difference and the laminar flow with a change to turbulent flow at the exit point. The red region shows how the velocity is higher at the outlet of the enclosure.

In Table 1 presents data related to normal filters, showing the relationship between hydraulic diameter (*Dh*), porosity (ϵ), and heat flux (*q*). diameter (*Dh*) Represents the hydraulic diameter, a measure of the characteristic length used for fluid flow in porous media. It's often calculated based on geometry and cross-sectional area. porosity (ϵ), Indicates the fraction of the filter's volume that is void space, allowing fluid to flow through. Higher values of porosity imply that the filter has more open space, which affects both fluid and heat transport properties.

Table.2 presents data related to ULPA (Ultra-Low Particulate Air) and HEPA (High-Efficiency Particulate Air) filters, showing the relationship between hydraulic diameter (*Dh*) porosity (ϵ) and heat flux (*q*).

Table.2. Comparison between conventional filters and ULPA & HEPA Filters.

$Dh(m)$	ULPA and HEPA Filters	
	Porosity(ϵ)	Heat flux(q) W/m^2
1	0.7	0.018
2	0.73	0.0189
3	0.76	0.0195
4	0.8	0.02
5	0.85	0.04
6	0.89	0.065

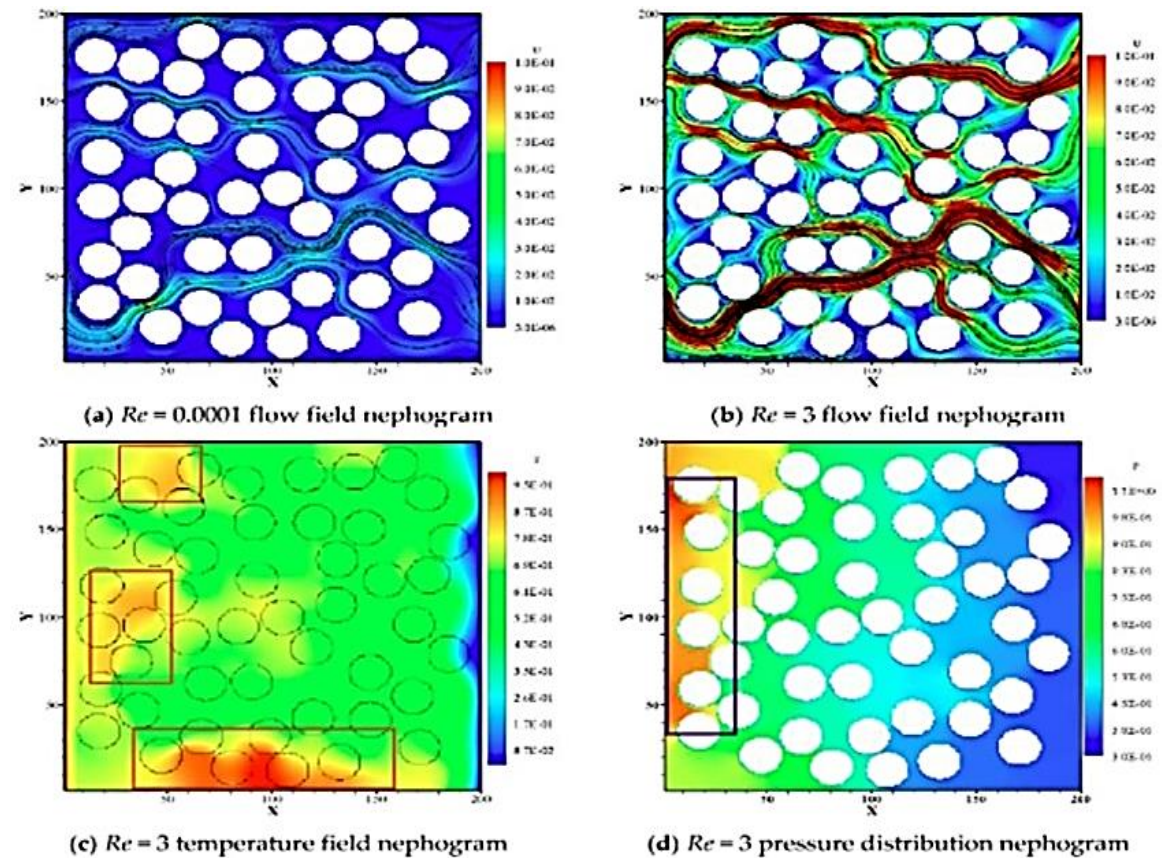


Figure 6. Nephogram representation.

Higher porosity in ULPA and HEPA filters improves both airflow and heat transfer capabilities, making them suitable for applications requiring high efficiency in particle filtration and thermal management. The nonlinear relationship between porosity and heat flux suggests that optimizing filter design (e.g. material selection and structure) can significantly enhance performance. These filters are ideal for industries like clean rooms, healthcare, electronics manufacturing and HVAC systems, where both filtration efficiency and heat dissipation are critical.

Figure 6.illustrate the dispersion or traversal of fluids, be they gases or liquids, through a porous medium. Such porous enclosures are oft encountered in divers engineering and environmental contexts, encompassing porous materials employed in filtration systems, subterranean aquifers, or layers of soil. In this regard, a nephogram does depict parameters such as fluid flow velocity, pressure distribution, or concentration gradients within the porous medium. It doth provide profound insights into the manner by which fluids percolate through the porous structure, a matter of utmost import for comprehending processes such as filtration, the flow of groundwater, or the conveyance of contaminants within the soil.

CONCLUSIONS AND SCOPE

Verily the present inquiry hath delved into the matter of natural convection within porous filters, contrasting the regular filter against the ULPA and HEPA variants. Through diligent numerical analysis, we have derived conclusions thus:

1. Within the bounds of Rayleigh numbers betwixt 2000 and 4000, natural convection doth reign supreme. In this realm, the airflow doth exhibit qualities both of laminar and turbulent flow, thereby engendering a remarkable augmentation in Heat flux.
2. The disparity in Heat flux betwixt the normal filters and the ULPA and HEPA brethren doth approximate threefold, with the latter exhibiting significantly loftier values of Heat flux.
3. At the portal, pressure doth stand high whilst velocity abides low; yet upon the egress, turbulence doth manifest, and through convergence, a decrement in pressure and a concomitant rise in velocity are observed.
4. The zenith and nadir of Heat flux engendered by ULPA and HEPA filters do the range betwixt 0.018 and 0.065 W/m² at mid porosity levels spanning from 0.4 to 0.6.
5. The correlation betwixt permeability and grid number doth serve to authenticate and refine numerical models, ensuring their fidelity in replicating the fluidic compartments of the material realm.

Scope and Future Work

Composite porous heat transfer materials are gaining attention due to their unique properties, which combine high thermal conductivity with low density and the ability to manage heat effectively. The future scope for these materials is promising, with potential applications across various industries and areas of research. Here are some key directions for future development:

- *Thermal energy storage (TES)*: Composite porous materials could enhance TES systems by improving heat transfer rates and energy storage capacity, particularly in concentrated solar power plants and other renewable energy systems.
- *Phase change materials (PCMs)*: These materials can be used to create more efficient PCMs, which are critical for storing and releasing thermal energy in applications like thermal management systems in electronics, buildings, and vehicles.
- *Microelectronics and high-power devices*: As electronic devices become more powerful and compact, effective cooling solutions are essential. Composite porous materials could be used in heat sinks and thermal interface materials to dissipate heat more efficiently, thereby improving the performance and lifespan of electronic components.
- *Data centers*: With the rising demand for data centers, which generate significant amounts of heat, there is a need for innovative cooling solutions. Composite porous materials could offer improved thermal management for data centers, reducing energy consumption and operational costs.
- *Lightweight thermal management*: The aerospace and automotive industries demand materials that are both lightweight and efficient in heat transfer. Composite porous materials could be used in these sectors to develop lighter, more efficient thermal protection systems for spacecraft, aircraft, and high-performance vehicles.
- *Battery thermal management*: In electric vehicles (EVs), managing battery temperature is crucial for safety and efficiency. Composite porous materials could be used to enhance battery thermal management systems, extending battery life and performance.
- *Implantable devices*: Composite porous materials with tailored thermal properties could be used in biomedical implants to better manage heat generated by electronic components, improving the safety and functionality of these devices.
- *Hyperthermia treatments*: In cancer treatment, controlled hyperthermia is used to kill cancer cells. Composite porous materials could be developed to optimize the delivery of heat to specific areas within the body.
- *Insulation*: Composite porous materials could be used to create high-performance insulation materials that offer better thermal management while being environmentally friendly and sustainable.

- *Energy-efficient facades*: These materials could be integrated into building facades to improve thermal regulation, reducing the need for heating and cooling and contributing to energy-efficient building designs.
- *3D Printing*: The development of additive manufacturing techniques could enable the production of highly customized composite porous materials with complex geometries, optimized for specific heat transfer applications.
- *Nanotechnology*: Incorporating nano materials into composite porous structures could further enhance their thermal properties, leading to breakthroughs in various applications, from electronics to aerospace.
- *Heat exchangers in renewable energy systems*: Composite porous materials could be used to design more efficient heat exchangers for renewable energy systems, such as geothermal and solar thermal plants.
- *Water desalination*: These materials could be used in solar stills and other desalination technologies, improving the efficiency of water purification processes through better heat transfer and evaporation rates.
- *Material optimization*: Ongoing research into new composite formulations and the understanding of heat transfer mechanisms in porous structures could lead to the development of materials with even better performance characteristics.
- *Multi-functional materials*: Future developments may focus on creating multi-functional materials that not only manage heat but also offer additional benefits such as electrical conductivity, structural strength, or chemical resistance.

CONCLUSION

The future scope for composite porous heat transfer materials is vast and multifaceted. As industries continue to push the boundaries of what is possible with heat management, these materials will likely play a critical role in enabling new technologies and improving existing ones. The integration of advanced manufacturing techniques and material science innovations will further expand their potential applications, making them a key area of focus for researchers and engineers in the coming years.

Table 3. Nomenclature

Nomenclature			
μ_e	Effective fluid viscosity	<i>ULPA</i>	Ultra-Low penetration air filter
K	thermal conductivity, $\text{W m}^{-1} \text{K}^{-1}$	<i>HEPA</i>	High Efficiency particulate air filter
V	Fluid velocity	<i>Greek symbols</i>	
μ	Fluid viscosity	α	thermal diffusivity, $\text{m}^2 \text{s}^{-1}$
Nu_{Local}	local Nusselt number	β	volume expansion co-efficient, K^{-1}
\overline{Nu}	average Nusselt number	ε	Porosity
P	dimension less pressure	θ	dimensionless temperature
P	Pressure drop	γ	kinematic viscosity, $\text{m}^2 \text{s}^{-1}$
Ra	Rayleigh number	ρ	density, kg m^{-3}

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